

# **How does groundwater flow ?**

February 26, 2002

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# Definitions

- ⇒ Unconfined Aquifer
- ⇒ Confined Aquifer
- ⇒ Water Table
- ⇒ Piezometric surface
- ⇒ Ground water well
- ⇒ Piezometer
- ⇒ Pumping well

# Unconfined aquifer

- ⇒ No confining layer at the top of the groundwater.  
Groundwater levels are free to rise or fall

# Confined aquifer

- ⇒ A layer of water bearing material that is sandwiched between two layers of much less conductivity (aquicludes or aquitards)

# Semi-confined aquifer

⇒ Confined aquifer that is “leaky”. Aquitards are not impermeable.

# Water Table

- ⇒ Top of an unconfined aquifer where pressure is equal to the atmospheric pressure ( $p = 0$ )
- ⇒ Also known as phreatic surface or free surface

# Piezometric Surface

- ⇒ The surface obtained by connecting equilibrium water levels in piezometers penetrating the confined aquifer



# Groundwater well

⇒ Measures the level of the water table

# Piezometer

- ⇒ Measures the level of the piezometric surface (or, in other words, measures the pressure at a point in a confined or semi confined aquifer)

# Pumping Well

- ⇒ Well used to pump water from a confined or unconfined aquifer to the surface. Can be screened over multiple depths, and pump from multiple aquifers

# Definitions

- ⇒ Transmissivity
- ⇒ Storativity
- ⇒ Specific Yield
- ⇒ Safe Yield

# Transmissivity

⇒ Hydraulic Conductivity \* Thickness of Aquifer

$$\Rightarrow K * B = T$$

# Specific Storage

- ⇒ Volume of water that a unit volume [of a porous medium] releases from (or takes into) storage when the pressure head in the unit volume [of a porous medium] changes a unit amount
- ⇒ Also known as the storage coefficient in a confined aquifer

# Specific Yield

- ⇒ Also known as 'storativity' or 'storage coefficient' in unconfined aquifer
- ⇒ Ratio of the volume of water that drains by gravity to the total volume of the porous media

# Safe Yield

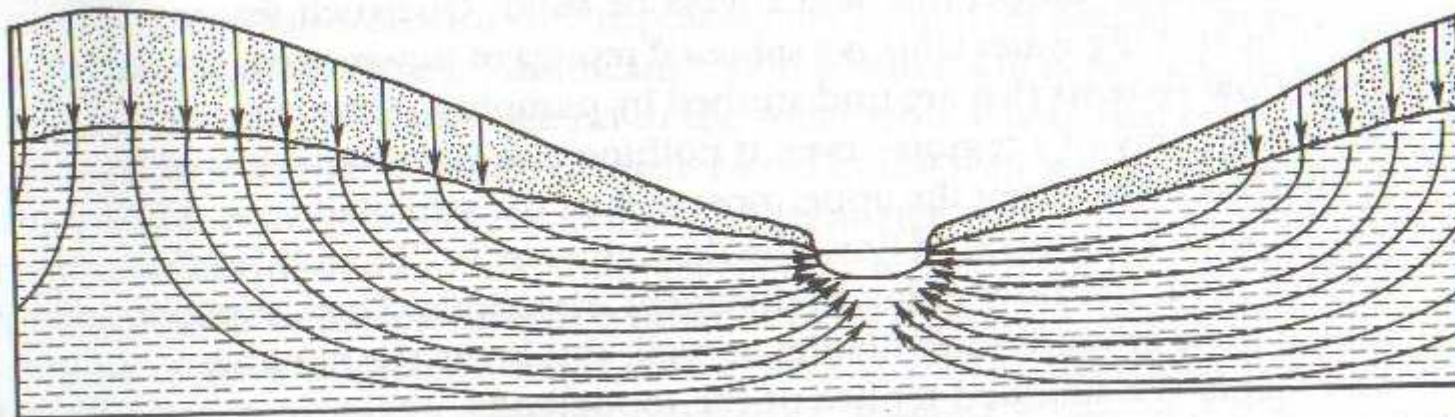
- ⇒ Economic term: Sustainable levels of water extraction...



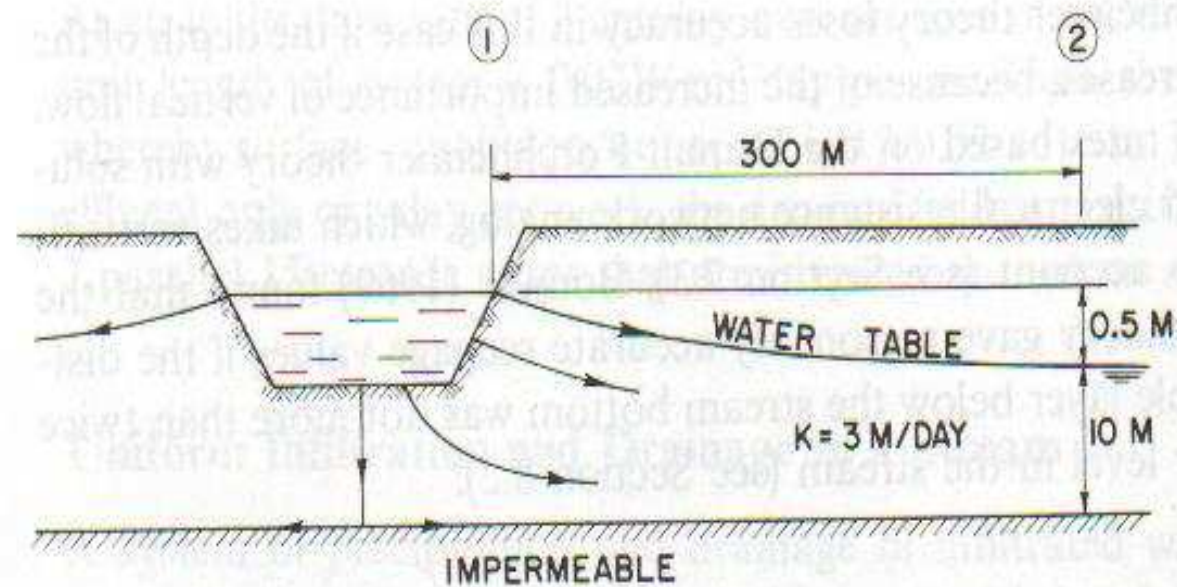
# How does groundwater flow?

⇒ Darcy: Hydraulic Gradient

⇒ Velocity vs Flux

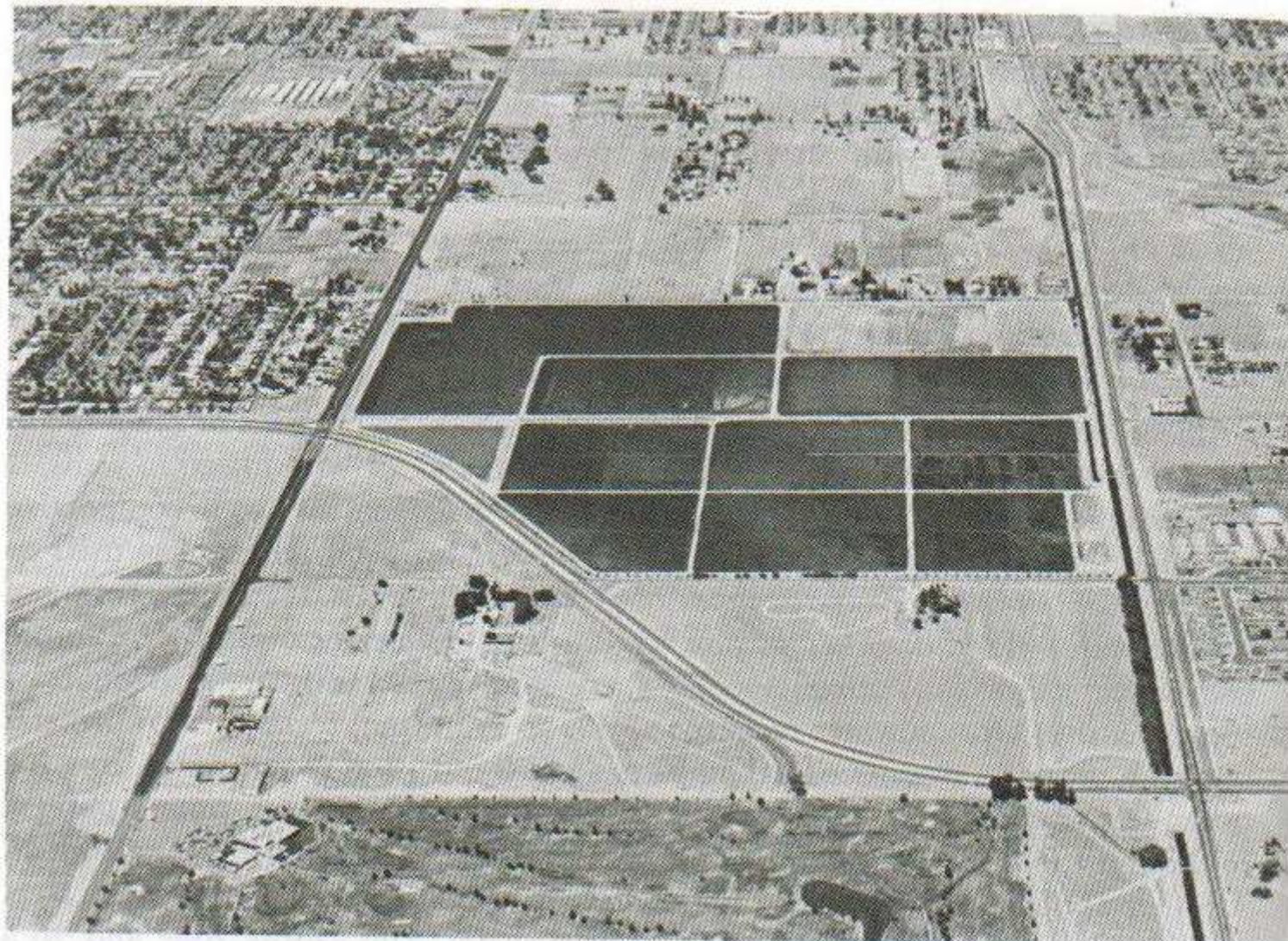


**Figure 7.2**  
Diagrammatic section illustrating ground water flow in a watershed (from King, 1899).



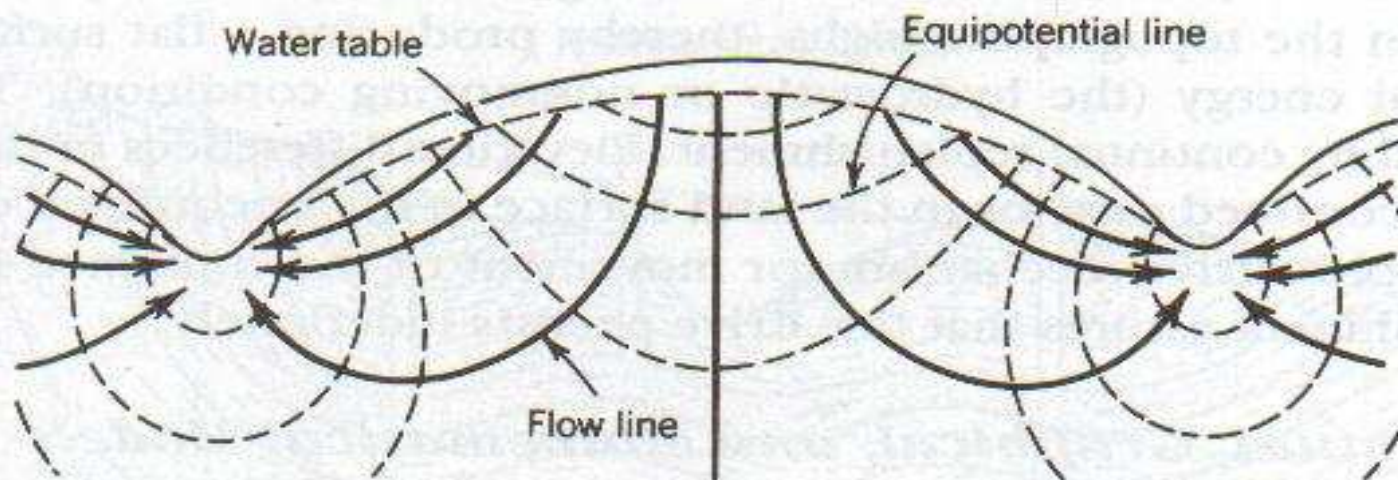
**Figure 3.7** Seepage from stream in unconfined aquifer with impermeable layer at relatively shallow depth.





**Figure 8.16** Leaky-Acres groundwater recharge project in Fresno, California. (*Photograph courtesy of U.S. Department of Agriculture.*)





**Figure 7.3**

Topographically controlled flow pattern (from Hubbert, 1940). Reprinted by permission of the Journal of Geology, University of Chicago Press. Copyright © 1940.



# **Wells and well screening**

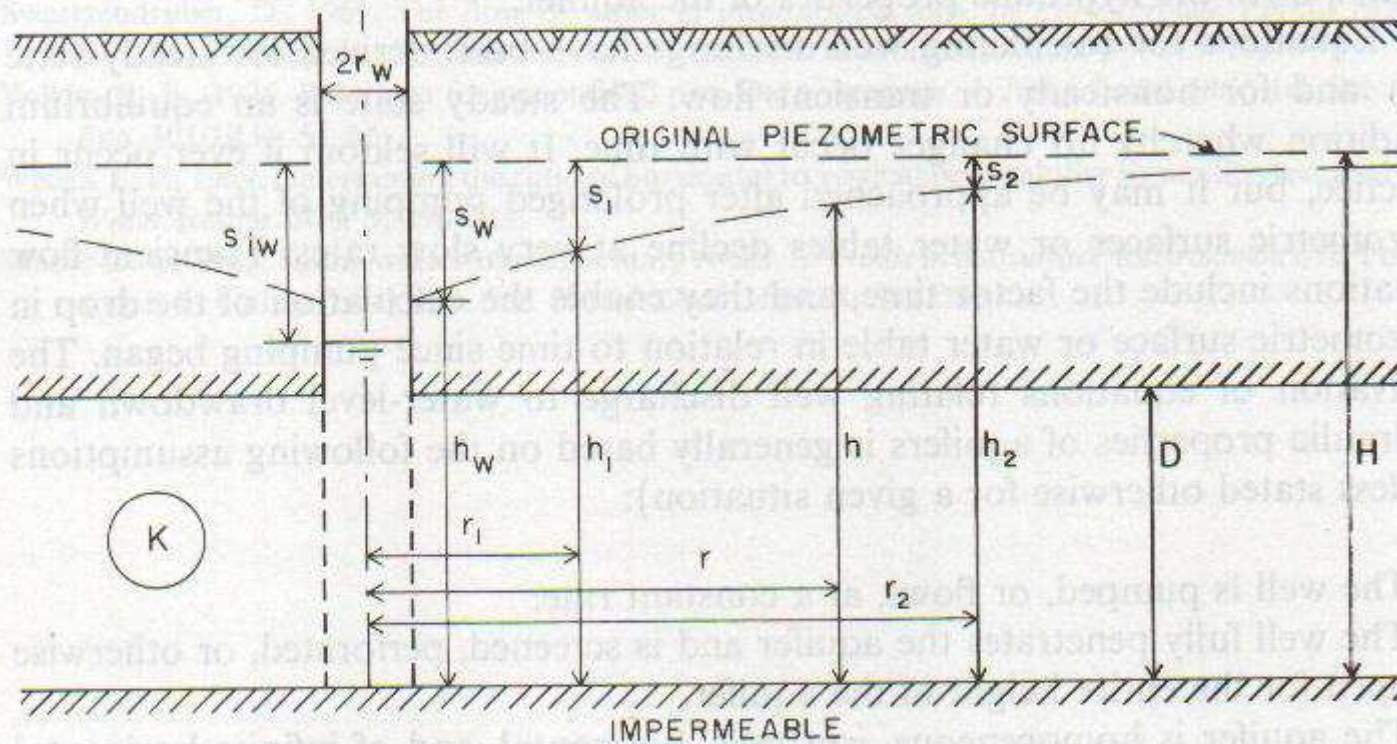
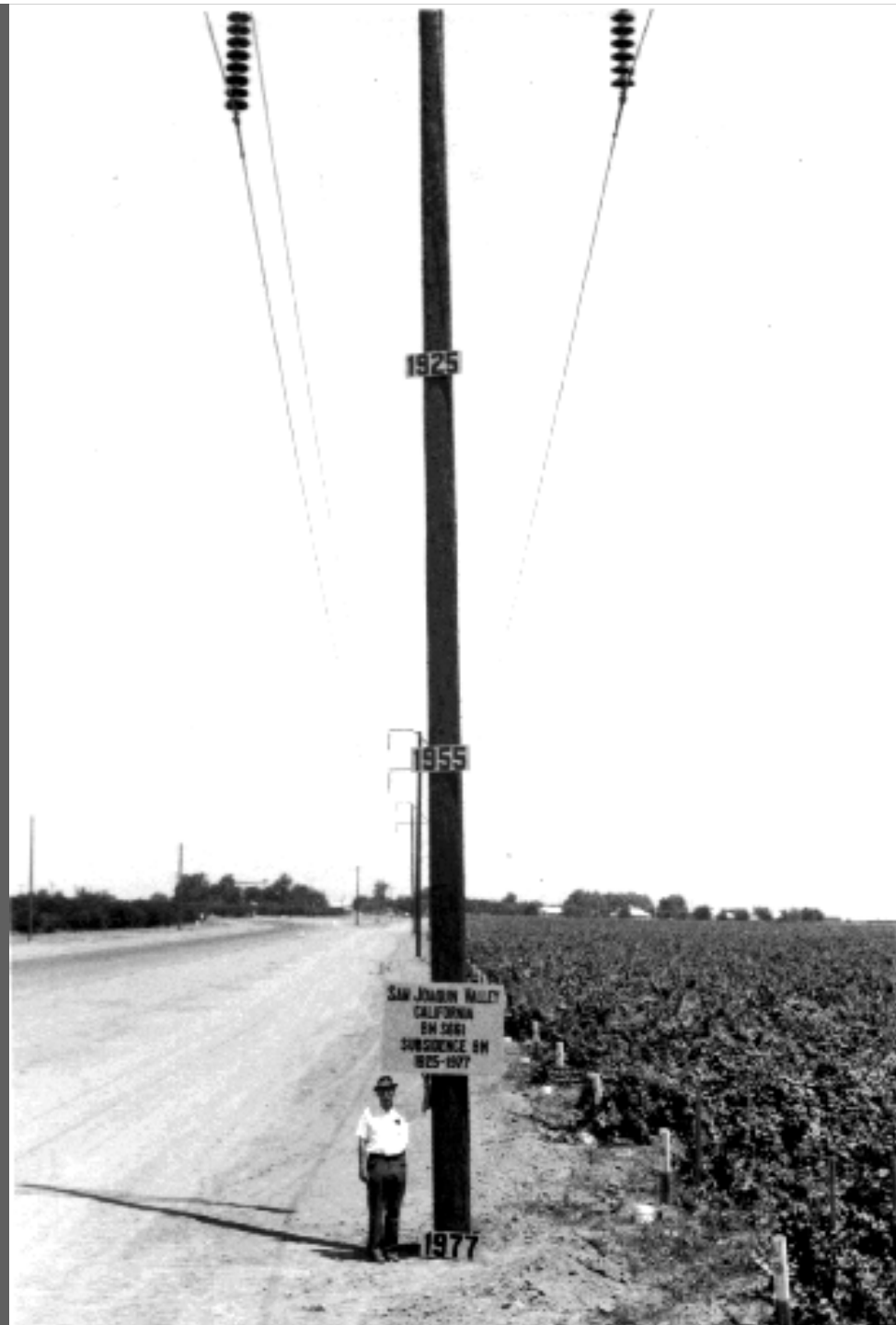


Figure 4.1 Geometry and symbols for pumped well in confined aquifer.



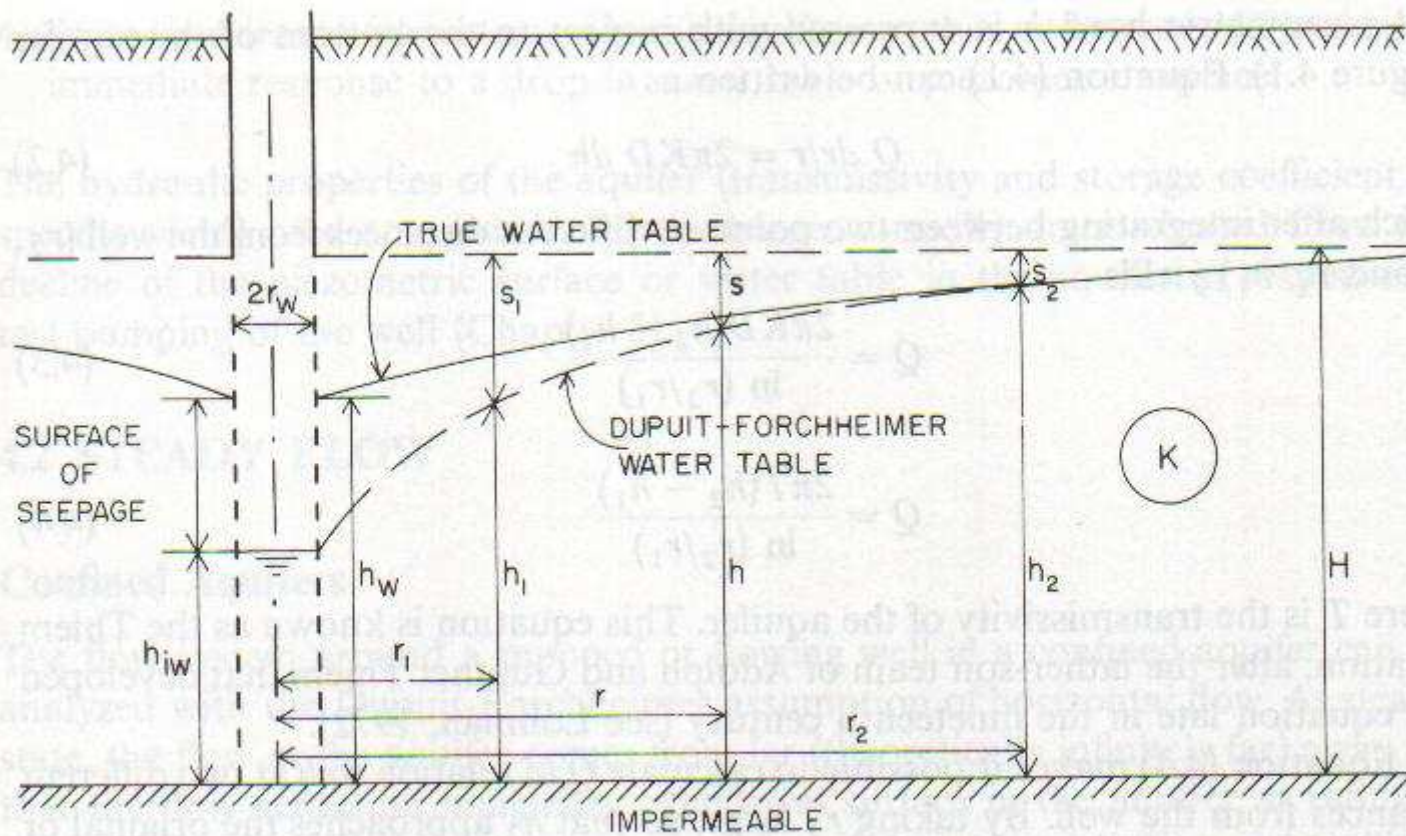


1925

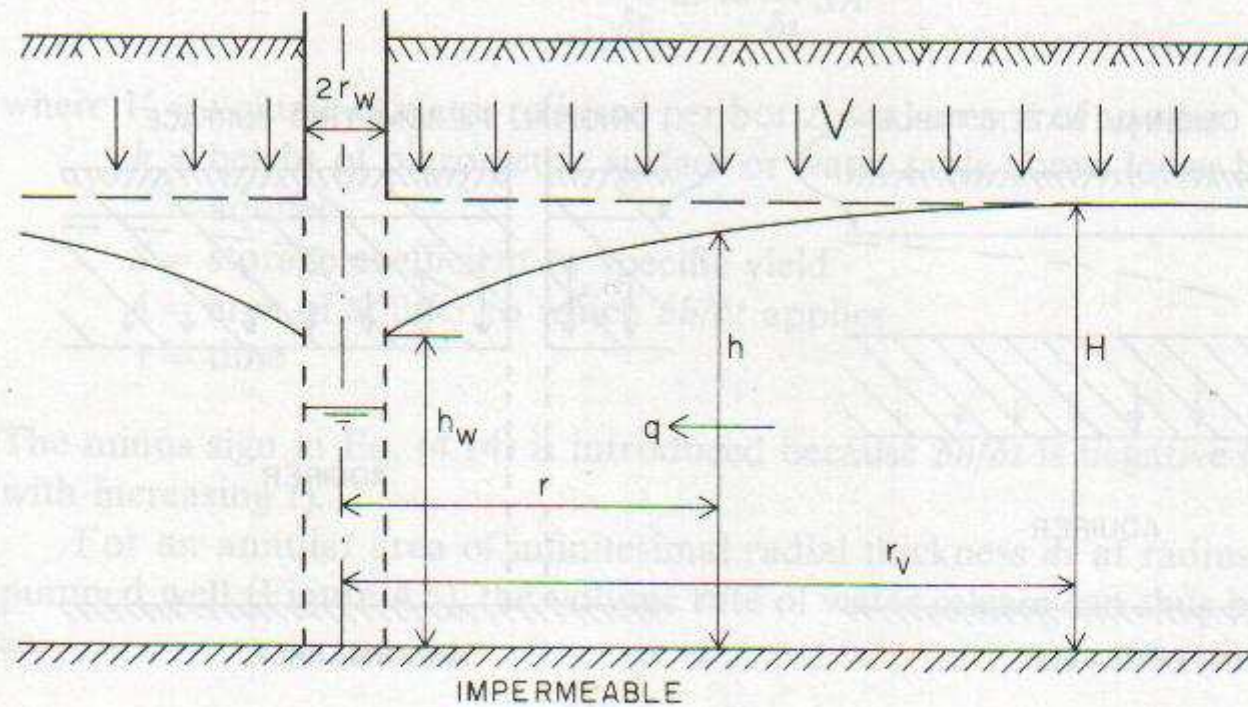
1955

SAN JOAQUIN VALLEY  
CALIFORNIA  
6M 60K1  
SUBSTANCE 6M  
1925-1977

1977



**Figure 4.2** Geometry and symbols for pumped well in unconfined aquifer.



**Figure 4.3** Pumped well in unconfined aquifer in equilibrium with vertical recharge.



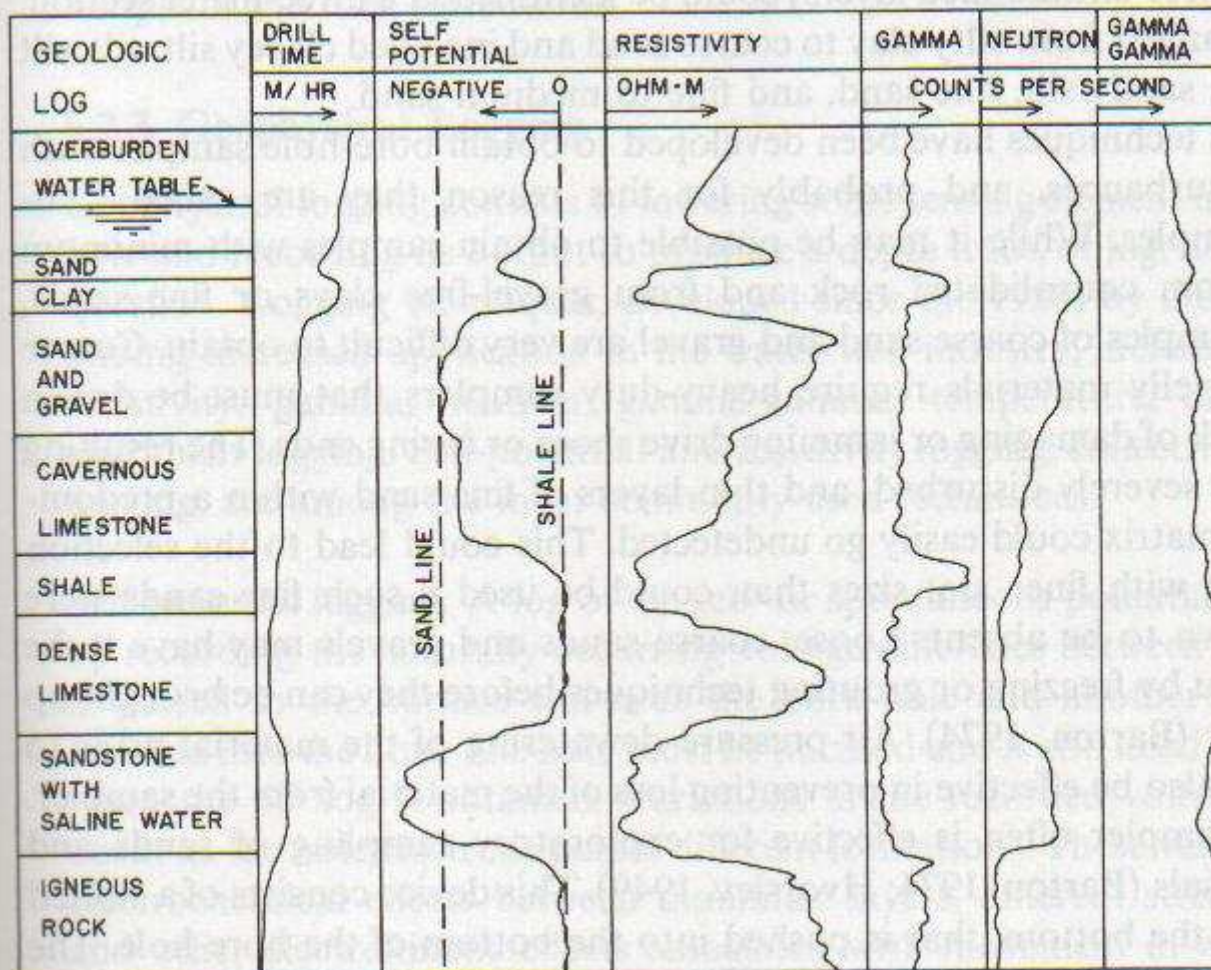
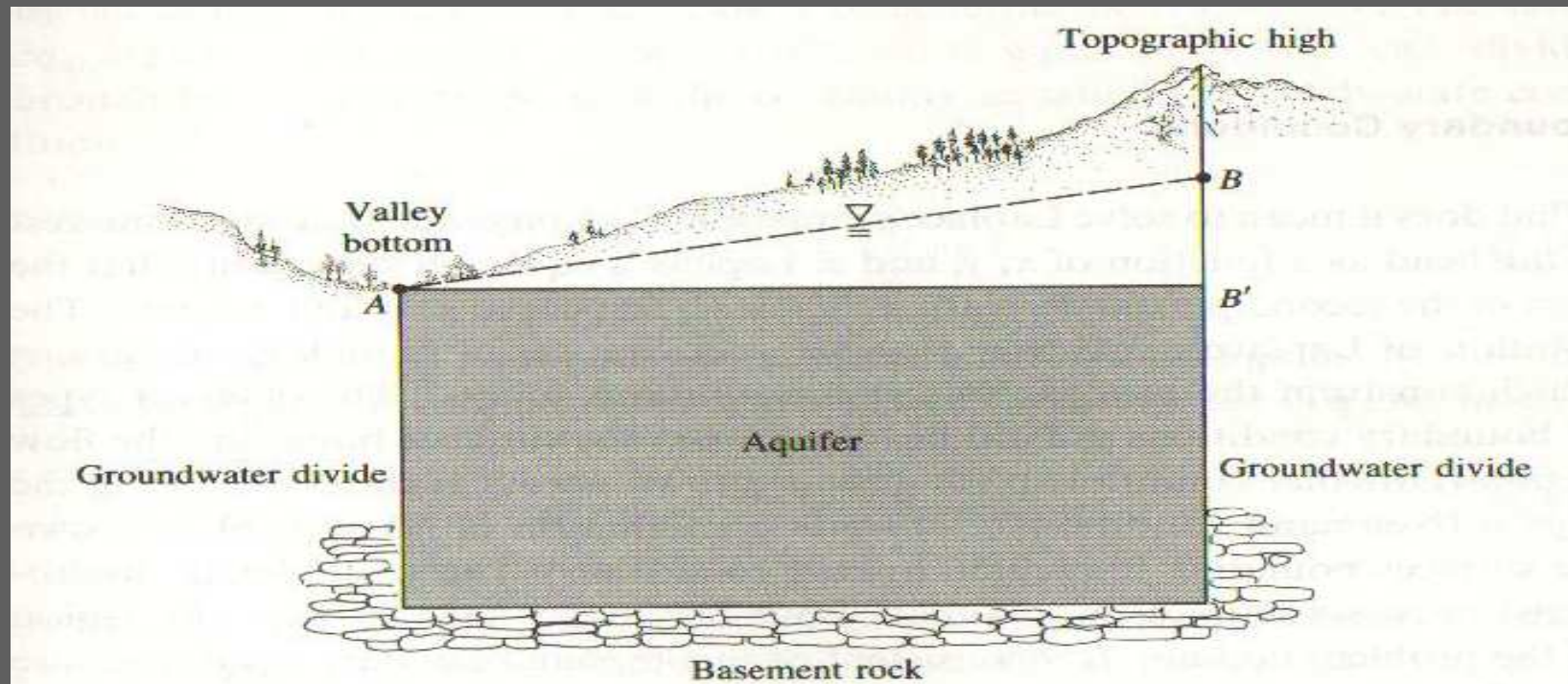


Figure 6.5 Hypothetical driller's and geophysical logs.



**Figure 1.6**  
Schematic representation of the boundaries of a two-dimensional regional groundwater flow system.

# Continuum ... Remember this ?

$$-\left(\frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} + \frac{\partial q_z}{\partial z}\right) = 0$$

**OR**

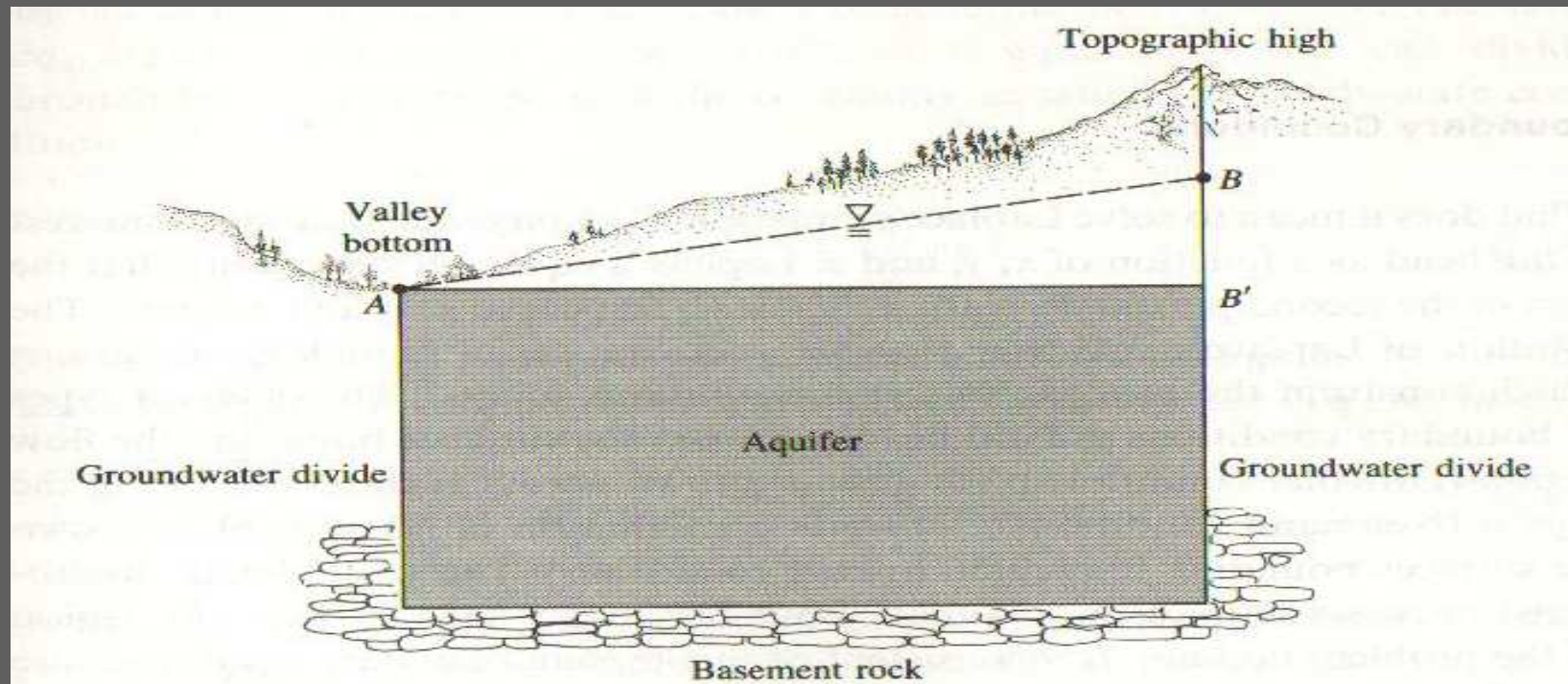
$$\frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} + \frac{\partial q_z}{\partial z} = 0$$

## Combine with Darcy

$$0 = \frac{\partial}{\partial x} \left( K_x \frac{\partial H}{\partial x} \right) + \frac{\partial}{\partial y} \left( K_y \frac{\partial H}{\partial y} \right) + \frac{\partial}{\partial z} \left( K_z \frac{\partial H}{\partial z} \right)$$

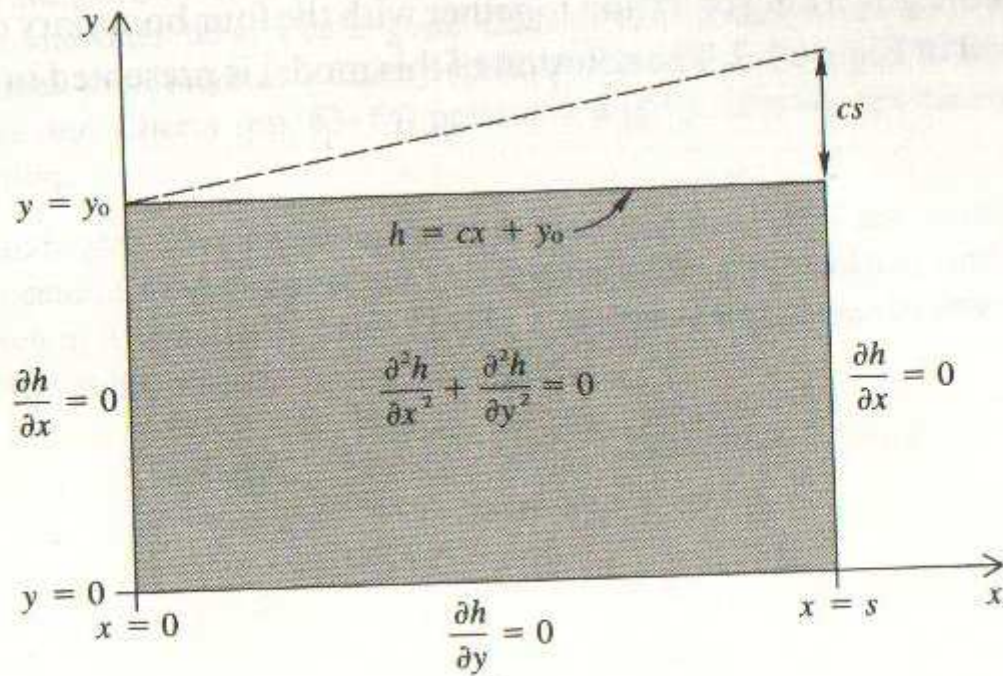
$$0 = \frac{\partial^2 H}{\partial x^2} + \frac{\partial^2 H}{\partial y^2} + \frac{\partial^2 H}{\partial z^2}$$





**Figure 1.6**  
Schematic representation of the boundaries of a two-dimensional regional groundwater flow system.





**Figure 1.7**  
 Mathematical model of the regional groundwater flow system shown in Figure 1.6.

# Boundary Conditions

- ⇒ No flow boundary
- ⇒ Dirichlet boundary
  - Head is known for surfaces bounding the flow region
- ⇒ Neumann boundary
  - Flow is known across surface bounding the region
- ⇒ Combined head/flow knowledge